

a) the Volume change

$$v_{fg} = v_g - v_f$$

$$= (1.6941) - (0.001043)$$

$$= 1.6931 \text{ m}^3/\text{kg}$$

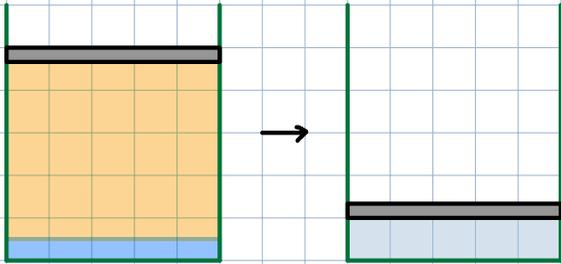
$$\Delta V = m v_{fg} = (0.2 \text{ kg}) \cdot (1.6931 \text{ m}^3/\text{kg})$$

$$= 0.3386 \text{ m}^3$$

b) the amount of energy transferred to the water

Energy  $\rightarrow$  the enthalpy of vaporization at that pressure

$$E = m h_{fg} = (0.2 \text{ kg}) \cdot (2257.5 \text{ kJ/kg}) = 451.5 \text{ kJ}$$



$T_1 = 25^\circ\text{C}$   
 $p_1 = 100\text{ kPa}$   
 air + liq. water (1 kg)  
 $V_1 = 1\text{ m}^3$

$T_2 = 180^\circ\text{C}$   
 air + water vapor  
 $V_2 = 0.1\text{ m}^3$

Air, ideal gas

$C_{v,air} = 0.728\text{ kJ/kg}\cdot\text{K}$   
 $R = 0.287\text{ kJ/kg}\cdot\text{K}$   
 $C_p - C_v = R$   
 $C_p = C_v + R$

- a) State 2 is ideal mixture  $\rightarrow p_2 = ?$   
 (Neglect any air dissolved in water)
- b)  $pV^n = \text{const} \rightarrow W = ?$
- c) Determine the heat transfer from the surrounding

(a) State 2 = air + water vapor

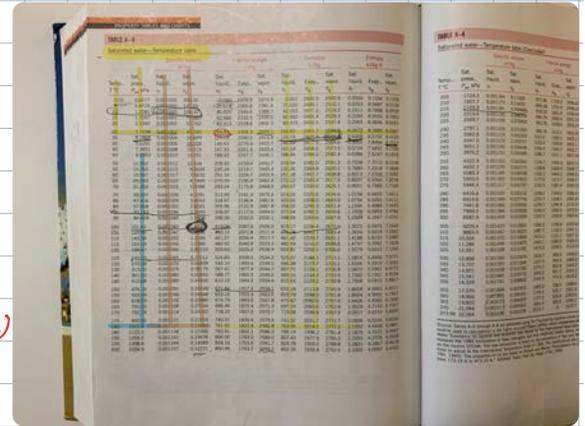
$p_2 = p_{2,air} + p_{2,wv}$   
 $p = nRT/V$

State 1: Table A-4:  $T_1 = 25^\circ\text{C} \rightarrow p_{\text{sat}} = 3.17\text{ kPa}$   
 air + liq. water  $\rightarrow p_1 = p_{1,wv} + p_{1,air} = 100\text{ kPa}$   
 $\therefore p_{1,air} = 96.83\text{ kPa}$

$p_1 V_1 = n R T_1 \rightarrow n = \frac{p_1 V_1}{R T_1}$  ( $\because$  volume occupied by liquid is neglected)

$m_{\text{air}} = \frac{(96.83\text{ kPa}) \cdot (1\text{ m}^3)}{(0.287\text{ kJ/kg}\cdot\text{K}) \cdot (298\text{ K})} = 1.13\text{ kg}$

State 2:  $p_2 V_2 = n R T_2$   
 $p_{2,air} = \frac{n R T_2}{V_2} = \frac{(1.13) \cdot (0.287) \cdot (453)}{(0.1)} = 1469.1\text{ kPa}$   
 $\rightarrow p_2 = (1469.1\text{ kPa}) + (1002.8) = 2471.9\text{ kPa}$  **Ans. (a)**  
 Table A-4:  $T_2 = 180^\circ\text{C} \rightarrow p_{2,wv} = 1002.8\text{ kPa}$



(b)  $pV^n = \text{const} \rightarrow W = ?$

$W = \int_{V_1}^{V_2} p dV \leftarrow pV^n = C$   
 $= \frac{p_2 V_2 - p_1 V_1}{1-n}$   
 $= \frac{(2471.9)(0.1) - (100)(1)}{1-1.393}$   
 $= -874.53\text{ kJ}$

$p_1 V_1^n = p_2 V_2^n$   
 $(100) \cdot (1)^n = (2471.9) (0.1)^n$   
 $(0.1)^n = 100 / 2471.9$   
 $n \cdot \log(0.1) = \log(100 / 2471.9)$   
 $\therefore n = 1.393$

**Ans (b)**

(c) Determine the heat transfer from the surrounding

Energy  $\rightarrow$  the enthalpy of vaporization

$$\Delta E = m h_{fg} = \Delta H = Q - W$$

$$Q = \Delta H + W$$

$$Q = \{\Delta H\}_{\text{air}} + \{\Delta H\}_{\text{wv}} + \{\Delta H\}_{\text{wl}} + W$$

$$m_{1,\text{wl}} = 1 \text{ kg} \longrightarrow V_2 = 0.1 \text{ m}^3$$

if all liq. water turned into sat. vapor,  $V_2 = 0.1 \text{ m}^3/\text{kg}$

$$\text{Table A-4: } T_2 = 180^\circ\text{C} \longrightarrow \begin{aligned} v_f &= 0.001127 \\ v_g &= 0.19384 \end{aligned}$$

$$\begin{aligned} v_2 &= \frac{V_2}{m} \\ v_g &= \frac{V_2}{m_{2,\text{wv}}} \longrightarrow m_{2,\text{wv}} = \frac{V_2}{v_g} = \frac{0.1 \text{ m}^3}{0.19384 \text{ m}^3/\text{kg}} = 0.51589 \text{ kg} \\ m_{2,\text{wl}} &= 1 - 0.51589 = 0.484 \text{ kg} \end{aligned}$$

$$\begin{aligned} \{\Delta H\}_{\text{air}} &= m_{\text{air}} \cdot C_p (T_2 - T_1) \leftarrow C_p = C_v + R \\ &= (1.13 \text{ kg}) \cdot (1.015 \text{ kJ/kg}\cdot\text{K}) \cdot (180 - 25 \text{ K}) \\ &= 177.78 \text{ kJ} \end{aligned}$$

$$\begin{aligned} \{\Delta H\}_{\text{wv}} &= m_{2,\text{wv}} \cdot h_{2,\text{wv}} - m_{1,\text{wv}} \cdot h_{1,\text{wv}} \leftarrow T = 180^\circ\text{C} \longrightarrow \begin{aligned} h_f &= 763.05 \\ h_{fg} &= 2014.2 \\ h_g &= 2777.2 \end{aligned} \\ &= (0.51589 \text{ kg}) \cdot (1802.16) \\ &= 929.73 \text{ kJ} \end{aligned}$$

$$\begin{aligned} \{\Delta H\}_{\text{wl}} &= m_{2,\text{wl}} \cdot h_{2,\text{wl}} - m_{1,\text{wl}} \cdot h_{1,\text{wl}} \\ &= (0.484) \cdot (763.05) - (1) \cdot (104.83) \\ &= 264.48 \text{ kJ} \end{aligned}$$

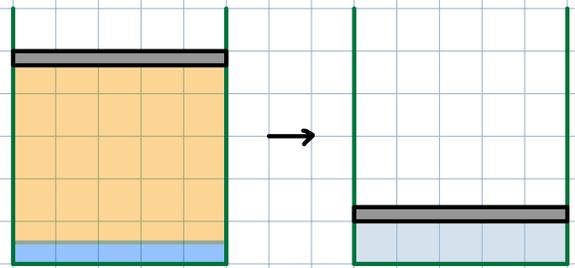
$$x_2 = \frac{0.51589 \text{ kg}}{1 \text{ kg}} = 0.51589 \longrightarrow h_{2,\text{wv}} = h_f + x_2 (h_{fg}) = 1802.16$$

$$Q = \{\Delta H\}_{\text{air}} + \{\Delta H\}_{\text{wv}} + \{\Delta H\}_{\text{wl}} + W$$

$$= (177.78) + (929.73) + (264.48) + (-374.53)$$

$$= 997.46 \text{ kJ}$$

Ans. (c)



$$T_1 = 25^\circ\text{C}$$

$$p_1 = 100 \text{ kPa}$$

air + liq. water (1 kg)

$$V_1 = 1 \text{ m}^3$$

$$T_2 = 180^\circ\text{C}$$

air + water vapor

$$V_2 = 0.1 \text{ m}^3$$